# MATHEMATICS (PART-I)

# **SOLUTION: PRACTICE QUESTION PAPER 1**

- **Q. 1. (A)** (i) (A)
  - (ii) (B)
  - (iii) (A)
  - (iv) (D).
  - Q. 1. (A) Explanation to the answers to MCQs in this question has been given below for students' guidance. Please note that, Students are not expected to write the explanation in the examination.

**Explanations:** 

- (i) Substitute y = 3 in the given equation.
- (ii) d = (x+3) (x-1) = (3x+1) (x+3)

Solving simple equations, find the value of x. Hence, find the value of d.

- (iii) There are 8 cards bearing numbers multiple of 5 from cards 1 to 40.
- (iv) Use the formula :  $\alpha + \beta = \frac{-b}{a}$ .
- Q. 1. (B) (i) Solution:

FV = ₹ 100, MV = ₹ 150, Dividend = 10%

Shweta purchased 5 shares of FV ₹ 100.

Dividend = 10% = ₹ 10 per share of FV ₹ 100.

 $\therefore$  dividend on 5 shares =  $\mathbf{\xi}$  10  $\times$  5 =  $\mathbf{\xi}$  50

**Ans.** Shweta gets dividend ₹ 50.

# (ii) Solution:

$$4y = 12 - 3x$$

$$\therefore 4y + 3x - 12 = 0$$

i.e. 
$$3x + 4y - 12 = 0$$

Ans. The general form is 3x + 4y - 12 = 0.

(iii) Solution:

Let 
$$\alpha = -3$$
 and  $\beta = -5$ 

$$\alpha + \beta = -3 + (-5) = -8;$$
  $\alpha \beta = (-3) \times (-5) = 15$ 

The required quadratic equation is

$$x^2 - (\alpha + \beta) x + \alpha \beta = 0$$

i.e. 
$$x^2 - (-8)x + 15 = 0$$
 i.e.  $x^2 + 8x + 15 = 0$ 

Ans. The quadratic equation is  $x^2 + 8x + 15 = 0$ .

# (iv) Solution:

$$S = \{1, 2, 3, 4, 5, 6\}$$

Event 
$$A = \{1, 3, 5\}$$

**Ans.** Event  $A = \{1, 3, 5\}$ .

### Q. 2. (A) (i) Activity:

x	4	-1	0
у	0	-5	-4
(x, y)	(4, 0)	(-1, -5)	(0, -4)

$$[x-y=4]$$

$$\therefore 4-v=4$$

$$\therefore 4 - y = 4 \qquad \qquad \dots \text{ (Substituting } x = 4\text{)}$$

$$\therefore -y = 4 - 4$$
  $\therefore -y = 0$  i.e.  $y = 0$ 

$$\therefore -y=0$$

i.e. 
$$v = 0$$

$$x-y=4$$

$$\therefore x - (-5) = 4$$

... (Substituting 
$$y = -5$$
)

$$\therefore x + 5 = 4$$
  $\therefore x = 4 - 5$  i.e.  $x = -1$ 

$$\therefore x = 4 - 5$$

i.e. 
$$x = -1$$

$$x-y=4$$

$$\therefore 0-y=4$$

... (Substituting 
$$x = 0$$
)

$$\therefore -y = 4$$

$$\therefore y = -4.$$

# (ii) Activity:

Here, a = 1, d = 2,  $t_n = 149$ 

$$t_n = a + \boxed{(n-1) \ d}$$

$$t_n = a + \boxed{(n-1) \ d}$$
 ... (Formula)  
 $\therefore 149 = \boxed{1 + (n-1) \times 2}$  ... (Substituting the values)

$$\therefore 149 = 2n - \boxed{1}$$
 \tag{75}.

$$\therefore n = 75.$$

# (iii) Activity:

If two coins are tossed simultaneously.

$$S = \left\{HH, \boxed{HT}, \boxed{TH}, TT\right\}$$

(i) Event A: at least getting one head.

$$\therefore A = \left\{ HH, \boxed{\mathbf{HT}}, TH \right\}$$

(ii) Event B: to get no head.

$$\therefore B = \left\{ \boxed{\mathbf{TT}} \right\}.$$

### Q. 2. (B) (i) Solution:

$$4x + 3y = 11$$

$$3x + 4y = 10$$

Multiplying equation (1) by 4,

$$16x + 12y = 44$$
 ... (3)

Multiplying equation (2) by 3,

$$9x + 12y = 30$$
 ... (4)

Subtracting equation (4) from equation (3),

$$16x + 12y = 44$$
 ... (3)

$$9x + 12y = 30$$
 ... (4)

$$7x = 14$$

$$\therefore x = 2$$
 ... (Dividing both the sides by 7)

Substituting x = 2 in equation (1),

$$4(2) + 3v = 11$$
  $\therefore 8 + 3v = 11$   $\therefore 3v = 11 - 8$ 

$$3 + 3y = 11$$

$$\therefore 3y = 11 - 8$$

$$\therefore 3y = 3$$

$$\therefore y = 1$$

... (Dividing both the sides by 3)

Ans. (x, y) = (2, 1) is the solution.

### (ii) Solution:

Comparing the equation  $2x^2 - 7x - 2 = 0$  with  $ax^2 + bx + c = 0$ ,

$$a = 2, b = -7, c = -2$$

$$\Delta = b^2 - 4ac = (-7)^2 - 4 (2) (-2)$$

$$=49+16=65$$

Here,  $\Delta > 0$ 

**Ans.** The roots are **real and unequal**.

#### (iii) Solution:

For getting 1 share of FV ₹ 100, the investment is ₹ 120.

Dividend = 15% = ₹ 15 per share of ₹ 100.

Rate of return = 
$$\frac{\text{Dividend income}}{\text{Sum invested}} \times 100$$
  
=  $\frac{15}{120} \times 100 = 12.5$ 

Ans. The rate of return for Amol is 12.5%.

[Note: To find the rate of return, the numbers of share purchased is immaterial.]

#### (iv) Solution:

Here, 
$$a = t_1 = 5$$
,  $t_{10} = 95 = t_n$ ,  $S_{10} = ?$ 

$$S_n = \frac{n}{2} [t_1 + t_n] \qquad \dots \text{ (Formula)}$$

... 
$$S_{10} = \frac{10}{2} [5 + 95]$$
 ... (Substituting the values)  
=  $5 \times 100$   
...  $S_{10} = 500$   
**Ans.**  $S_{10} = 500$ .

#### (v) Solution:

Here, 
$$L = 60$$
,  $h = 20$ ,  $f_1 = 100$ ,  $f_0 = 70$ ,  $f_2 = 80$   
Mode  $= L + \left[ \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$   
 $= 60 + \left[ \frac{100 - 70}{2 \times 100 - 70 - 80} \right] \times 20$   
 $= 60 + \frac{30}{200 - 150} \times 20$   
 $= 60 + \frac{30}{50} \times 20$   
 $= 60 + 12 = 72$ 

Ans. Mode is 72.

## Q. 3. (A) (i) Activity:

Here, 
$$a = 1$$
,  $b = -10$ ,  $c = -24$   

$$b^{2} - 4ac = (-10)^{2} - 4 \times 1 \times (-24) = 100 + 96 = 196$$

$$x = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a} = \frac{-(-10) \pm \sqrt{196}}{2 \times 1} = \frac{10 \pm 14}{2}$$

$$x = 12 \text{ or } x = -2$$

 $\therefore x = 12$  or x = -2.

#### (ii) Activity:

The cumulative frequency which is just greater than 125 is 153

 $\therefore$  the corresponding class |150-200| is the median class.

$$L = 150, f = 90, cf = \boxed{63}, h = 50$$

Median = 
$$L + \left[\frac{\frac{N}{2} - cf}{f}\right] \times h$$
  
=  $150 + \left[\frac{125 - 63}{90}\right] \times 50$   
=  $150 + \frac{62}{90} \times 50 \approx 184.4$ 

The median data is 184.4 mangoes.

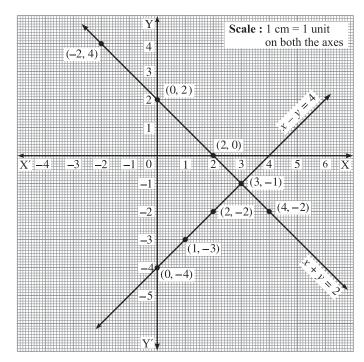
#### Q. 3. (B) (i) Solution:

$$x + y = 2 \qquad \therefore y = 2 - x$$

х	<b>-2</b>	0	2	4
У	4	2	0	- 2
(x, y)	(-2, 4)	(0, 2)	(2, 0)	(4, -2)

$$x - y = 4$$
  $\therefore -y = 4 - x$   $\therefore y = x - 4$ 

х	0	1	2	3
У	<b>-4</b>	- 3	<b>-2</b>	<b>-</b> 1
(x, y)	(0, -4)	(1, -3)	(2, -2)	(3, -1)



The coordinates of the point of intersection are (3, -1).

Ans. The solution of the given simultaneous equations is x = 3 and y = -1.

# (ii) Solution: Let the cost price of the toy be $\overline{x}$ .

Gain is as much per cent as the cost price of the toy.

∴ gain = 
$$x\%$$
 of  $x = \frac{x}{100} \times x = ₹ \frac{x^2}{100}$ 

Cost price + gain = selling price

$$\therefore x + \frac{x^2}{100} = 24$$

Multiplying both the sides by 100,

$$100x + x^2 = 2400$$

$$\therefore x^2 + 100x - 2400 = 0$$

$$\therefore x^2 + 120x - 20x - 2400 = 0$$

$$\therefore x(x+120)-20(x+120)=0$$

$$-2400$$
+  $120 - 20$ 

$$(x + 120)(x - 20) = 0$$

$$\therefore x + 120 = 0$$

or 
$$x - 20 = 0$$

$$\therefore x = -120$$

or 
$$x = 20$$

But the price cannot be negative.

$$\therefore x = -120$$
 is unacceptable.  $\therefore x = 20$ 

$$x = 20$$

**Ans.** The cost price of the toy is  $\ge$  20.

(iii) Solution: Discount 5% of ₹ 1000 = 
$$\frac{5}{100} \times 1000 = ₹ 50$$

∴ taxable value = 
$$₹ (1000 - 50) = ₹ 950$$

Rate of GST = 5%

∴ GST = 
$$\frac{5}{100}$$
 × 950 = ₹ 47.50

Purchase price for the customer

= Taxable value + GST = ₹ 
$$(950 + 47.50)$$
 = ₹  $997.50$ 

**Ans.** The purchase price of the dress for the customer is ₹ 997.50.

#### (iv) Solution:

Time	Class mark	Frequency (Number	v f
(hours)	$(x_i)$	of students) (f <sub>i</sub> )	$x_i f_i$
0 - 2	1	10	10
2 - 4	3	16	48
4 – 6	5	20	100
6 – 8	7	4	28
Total		$\Sigma f_i = 50$	$\sum x_i f_i = 186$

Here, 
$$\Sigma x_i f_i = 186$$
,  $\Sigma f_i = 50$ 

Mean = 
$$\overline{X} = \frac{\sum x_i f_i}{\sum f_i} = \frac{186}{50} = 3.72$$

**Ans.** The mean time spent by the students for studies is **3.72 hours**.

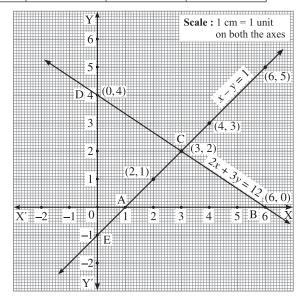
#### Q. 4. (i) Solution:

$$x-y=1$$
  $\therefore y=x-1$ 

x	2	4	6	
y	1	3	5	
(x, y)	(2, 1)	(4, 3)	(6, 5)	

$$2x + 3y = 12$$
  $\therefore y = \frac{12 - 2x}{3}$ 

X	0	3	6	
у	4	2	0	
(x, y)	(0, 4)	(3, 2)	(6, 0)	



From the graph (1)  $\triangle$  ABC is formed by the two lines and the X-axis.

(2)  $\triangle$  CDE is formed by the two lines and the Y-axis.

For  $\triangle$ ABC, AB = 5 units and the perpendicular drawn from point C on the X-axis is 2 units.

$$\therefore$$
 A( $\triangle$ ABC) =  $\frac{1}{2} \times 5 \times 2 = 5$  sq units.

For  $\triangle$  CDE, DE = 5 units and the perpendicular drawn from point C on the Y-axis is 3 units.

$$\therefore$$
 A( $\triangle$ CDE) =  $\frac{1}{2} \times 5 \times 3 = 7.5$  sq units.

**Ans.** The area of triangles are 5 sq units and 7.5 sq units respectively.

(ii) 
$$n(S) = 16$$
,  $n(R) = x$ .

Probability of getting a red ball

$$P_1(R) = \frac{n(R)}{n(S)} = \frac{x}{16}$$
 ... (1)

8 more red balls are put in the bag.

$$\therefore n(S) = 24, n(R) = (x + 8)$$

Probability of getting a red ball

$$P_2(R) = \frac{n(R)}{n(S)} = \frac{x+8}{24}$$
 ... (2)

From the given condition,

$$P_2(R) = 2 \frac{4}{9} P_1(R)$$

$$\therefore \frac{x+8}{24} = \frac{22}{9} \times \frac{x}{16}$$

Multiplying both the sides by 144,

$$6(x+8) = 22x$$

$$6x + 48 = 22x$$

$$\therefore 48 = 22x - 6x$$

$$\therefore 16x = 48$$

$$\therefore x = 3$$

**Ans.** Initially there were **3 red** balls in the bag.

## (iii) Solution:

$$15 + a + 30 + b + 15 + 10 = 100$$

$$a+b+70=100$$

$$a+b=100-70$$

$$\therefore a+b+70=100$$
  $\therefore a+b=100-70$   $\therefore a+b=30$  ... (1)

Now, a = 2b Substituting the value of a in equation (1),

$$2b + b = 30$$
  $\therefore 3b = 30$   $\therefore b = 10$ 

$$3b = 30$$

$$b = 10$$

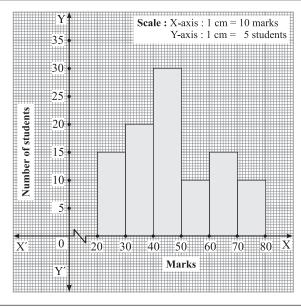
$$a = 2b = 2 \times 10 = 20$$
 :  $a = 20$ 

$$\therefore a = 20$$

The value of a is 20 and that of b is 10.

Tabulation for histogram:

Marks	20-30	30-40	40-50	50-60	60-70	70-80	Total
Number of students	15	20	30	10	15	10	100



#### Q. 5. (i) Solution:

- (1) Let Payal's age be x years.
- (2) From the first condition, Sonal's age is (x + 12) years.
- (3) The reciprocal of Payal's age is  $\frac{1}{x}$  years and that of Sonal's age is  $\frac{1}{x+12}$  years.
- (4) The sum of the reciprocal of their ages is  $\frac{1}{2}$ .

$$\therefore \frac{1}{x} + \frac{1}{x+12} = \frac{1}{8}$$

$$\therefore \frac{x+12+x}{x(x+12)} = \frac{1}{8}$$

$$\therefore \frac{2x+12}{x^2+12x} = \frac{1}{8}$$

$$\therefore 8(2x+12) = x^2 + 12x$$

... (Cross multiplying)

$$16x + 96 = x^2 + 12x$$

$$\therefore x^2 + 12x - 16x - 96 = 0$$

$$x^2 - 4x - 96 = 0$$

$$\therefore x^2 - 12x + 8x - 96 = 0$$

$$\therefore x(x-12) + 8(x-12) = 0$$

$$\therefore (x-12)(x+8) = 0$$
  $\therefore x-12 = 0$  or  $x+8=0$ 

$$\therefore x = 12$$
 or  $x = -8$  But the age cannot be negative.

$$\therefore x = -8$$
 is unacceptable.  $\therefore x = 12$  and  $x + 12 = 12 + 12 = 24$ .

Ans. Payal's age is 12 years. Sonal's age is 24 years.

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#### (ii) Solution:

Let the first term of the A.P. be a and the common difference d.

Here, 
$$t_9 = 75$$
 and  $t_{21} = 183$ ,  $t_{15} = ?$ 

$$t_n = a + (n-1)d$$
 ... (Formula)

$$\therefore t_9 = 75 = a + (9 - 1)d$$
 ... (Substituting the values)

$$\therefore 75 = a + 8d$$
 ... (1)

Similarly, 
$$t_{21} = 183 = a + (21 - 1)d$$

$$\therefore 183 = a + 20d$$
 ... (2)

Adding equations (1) and (2),

$$a + 8d = 75$$
 ... (1)

$$a + 20d = 183$$
 ... (2)

$$2a + 28d = 258$$

$$\therefore a + 14d = 129 \qquad \qquad \dots \text{ (Dividing both the sides by 2) } \dots \text{ (3)}$$

Now, 
$$t_{15} = a + (15 - 1)d$$

$$\therefore t_{15} = a + 14d$$

$$\therefore t_{15} = 129$$
 ... [From (3)]

Ans. The 15th term of the A.P. is 129.

9